

### Introduction to flow in porous media - 2 credits

Course Number: 224.4039

**Lecturer**: Dr. Regina Katsman

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Course Type: Lecture

Course Level: MSc/ PhD

Prerequisites: No

#### **Course Description:**

The main objective of the course is to study a single- and two-phase flow of gas, oil and water within porous aquifers, and to define a coupling between them. The following subjects are covered: porous media, phase, phase saturation, permeability, relative permeability, phase compressibility; wettability, capillarity and capillary pressure, interphase phenomena (surface energy, surface tension, adhesion force); Darcy's law and diffusion equation in porous media; steady-state, quasi- steady-state, and transient flow regimes; two-phase flow of gas and oil in wells, flow regimes, flow maps of gas and oil, pressure drop; radial flow and well modeling; modeling, numerical solutions, simulations.

#### Topics:

- 1. Definitions: porous media, porosity (total and effective), grain packing, rock compressibility, hydrostatic vs. lithostatic pressure.
- 2. Fluid properties: phase, component, phase saturation, fluid density, density-pressure relation, fluid compressibility.
- 3. Fluid properties: gas solubility, mass fraction, fluid viscosity, phase saturation (initial and residual).
- 4. Interphase phenomena: surface energy, surface tension, interfacial tension, surface curvature and fluids pressure.
- 5. Interphase phenomena: wettability, capillarity and capillary pressure, Laplace equation for capillary pressure, Young's (contact angle) equation.
- 6. Interphase phenomena: capillary rise, phase adsorption, imbibitions, drainage, capillary entry pressure.
- 7. Residual and irreducible saturation, effective saturation, capillary pressure-saturation relations: Brooks Corey, van Genuchten, scaling.
- 8. Intrinsic and relative permeability, permeability-saturation relations for wetting and non-wetting phases: Brooks Corey, Corey, van Genuchten, Naar and Henderson's models, retention curve.
- 9. Darcy's flow: Darcy's experiment, volumetric flow rate, hydraulic conductivity, hydraulic potential, hydraulic head, pressure head, elevation head, hydrostatic vs. non hydrostatic loading.



- 10. Darcy's law (single phase): Darcy's velocity, average pore velocity, hydraulic conductivity and permeability, tortuosity, tortuosity-porosity relations, intrinsic permeability by Kozeny, Carman, Fair and Hatch, anisotropy.
- 11. Mass conservation for a single phase flow in porous media: representative elementary volume, different forms of a conservation equation, incompressible/slightly compressible/ compressible flow, initial and boundary conditions.
- 12. Two-phase flow of immiscible fluids: basic equations for saturation and pressure, mass conservation equation for each fluid phase, Darcy's velocities for each phase, non-linearity and coupling, initial and boundary conditions.
- 13. Alternative differential equations for fluid phase conservation: formulation in phase pressure and saturation, average formulation, weighted formulation.
- 14. General form of transport equation in continuum: advective and diffusive fluxes, Fick's law, particular cases of conservation equation: for a phase in a multiphase flow, for a component in a multi/single phase flow.

## **Learning Outcomes:**

At the end of the course, students will be able to:

- 1. Analyze transport processes in porous media.
- 2. Build reservoir simulators.
- 3. Simulate single- and two-phase flows in reservoirs.

**Requirements**: Attendance, two projects.

**Grading:** Passed – 65%, with grade.

# **Reading List:**

- 1. Pinder, G.F., Gray, W.G., 2008. Essentials of multiphase flow and transport in porous media. John Wiley & Sons, Inc., Hoboken, New Jersey.
- 2. Chen, Z., 2007. Reservoir Simulation Mathematical Techniques in Oil Recovery. Society for Industrial and Applied Mathematics, Philadelphia.