The nematocyst’s sting is driven by the tubule moving front

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The nematocyst is the explosive injection system of the phylum Cnidaria, and is one of the fastest delivery systems found in Nature. Exploring its injection mechanism is key for understanding predator–prey interactions and protection against jellyfish stinging. Here we analyse the injection of jellyfish nematocysts and ask how the build-up of the poly-γ-glutamate (pGlu) osmotic potential inside the nematocyst drives its discharge. To control the osmotic potential, we used a two-channel microfluidic system to direct the elongating nematocyst tubule through oil, where no osmotic potential can develop, while keeping the nematocyst capsule in water at all times. In addition, the flow inside the tubule and the pGlu concentration profiles were calculated by applying a one-dimensional mathematical model. We found that tubule elongation through oil is orders of magnitude slower than through water and that the injection rate of the nematocyst content is reduced. These results imply that the capsule’s osmotic potential is not sufficient to drive the tubule beyond the initial stage. Our proposed model shows that the tubule is pulled by the high osmotic potential that develops at the tubule moving front. This new understanding is vital for future development of nematocyst-based systems such as osmotic nanotubes and transdermal drug delivery.

1. Introduction

Nematocysts are ultra-fast stinging organelles that are utilized by most of the Cnidaria phylum (sea anemones, corals, jellyfish, hydra and myxozoans) for prey capture, defense strategies and locomotion [1–3]. Their unique structure and extremely fast penetration rates have fascinated scientists since the pioneering microscopy work of Antonie van Leeuwenhoek at the beginning of the eighteenth century. They are densely distributed along the tentacles and body surface, loaded and ready for firing [4]. Once fired, they cannot be used again, but, while still loaded, they can be effective even outside their biological cells [5].

A single nematocyst consists of a long thin needle-like tubule that is packed with a matrix inside the nematocyst capsule [4]. The tubule base is connected to the capsule wall and upon activation the tubule begins a fascinating inside-out eversion in which it elongates to reach a length of up to 100 times the capsule diameter. The capsule wall is composed of a mesh of proteins, cross-linked by intermolecular disulfide bridges, that provide the elasticity and tensile strength needed to withstand the extremely high internal pressure that drives the process [1,6,7]. The matrix is made of large aggregates of poly-γ-glutamate (pGlu) and metal cations [8,9]. It is initially trapped inside the capsule, but as water penetrates through the capsule wall the resulting aqueous pGlu solution leaves the capsule and fills up the tubule internal volume.

The common explanation suggests that an osmotic potential is building up inside the capsule owing to the pGlu matrix and the osmotic properties of the capsule wall [2,8–10]. According to this explanation, the osmotic potential generates the required forces to fire and elongate the tubule. It has been shown that,
as the process begins, the internal capsule pressure increases to 150 bars [11] and this high pressure drives the initial tubule acceleration, reported by Nächtet et al. [12] to be as high as $5 \times 10^6 \text{g}$ (where $g = 9.81 \text{ cm s}^{-2}$). The high pressure results in a temporary increase in the capsule diameter which quickly relaxes well before the tubule elongation is complete [11, fig. 3]. This extremely high tubule acceleration is utilized to penetrate prey targets such as fish scales and the tough cuticle of crustacean integuments. Past studies have focused on the triggering [13] and the initial few microseconds at the beginning of the tubule elongation process, overlooking the details of the rest of the process, and leaving the impression that the osmotic driven internal pressure in the capsule provides all the forces needed to complete the tubule elongation. However, a rough calculation shows that water penetrating the capsule through its wall dilutes the $\text{pGlu}$ solution such that the capsule loses most of its ability to continue pushing the tubule forward before its elongation is complete. Therefore, in addition to the capsule, another mechanism that can drive the tubule elongation must be identified. Hence, the study hypothesis is that the nematocyst tubule itself plays an important role in its own eversion. To test this hypothesis, we used a specially designed microfluidic platform to measure the elongation process while manipulating the osmotic potential along the tubule. The experimental findings were analysed by a mass transfer model developed here to represent the proposed elongation mechanism.

We begin by describing the experimental set-up and the mathematical model. We continue by presenting the results of the experiments conducted in water and in water–oil environments, the results of the model simulations and the results of the sensitivity analysis. The newly suggested explanation is discussed and its implications for drug delivery and other applications are presented.

2. Experimental methods

Tentacles from the jellyfish Rhopilema nomadica [14] were collected from Haifa Bay, Israel, and their large isorhiza nematocysts were isolated as described in Rachamim et al. [3] and activated with 1% subtilisin (Sigma). The nematocysts were trapped, activated and their elongation was measured in a microfluidic platform that was specially designed for this study (figure 1). The device consists of parallel micro-channels that bridge between two opposite wide channels. Channel 1 was filled with water and channel 2 was filled with oil for the water–oil experiments. As a control, both channels were filled with water for the water–water experiments. When injecting water into channel 1 and oil into channel 2, a water–oil interface was formed. As shown in figure 1c, its location was defined as the distance from the capsule to the water–oil interface, $L_{\text{oil}}$, and a few discharged nematocysts (not to scale).

Figure 1. The microfluidic platform: (a) a schematic of the microfluidic chip including the inlets and outlets, the two wide channels and the location of the micro-channels; (b) a microscopic image of the platform. The micro-channels in this chip are 50 $\mu\text{m}$ long and 5 $\mu\text{m}$ wide. (c) A representation of the 11 narrow micro-channels that connect between channel 1 and channel 2, the distance between the capsule and the water–oil interface, $L_{\text{oil}}$, and a few discharged nematocysts (not to scale).
technique [15], the structure of the microfluidic platform was fabricated on a silicon wafer using SU8 photoresist (SU-8 2025, Microchem, MA), and sealed on transparent glass slides. The hydrodynamic trapping principle [16, 17] was used in the design and the fabrication of these microfluidic devices to provide robust control over the introduction and exchange of the water, oil, capsule suspension and activator solution. Prior to each experiment, the microfluidic chip was filled with deionized water using a syringe pump (KDS LEGATO 210; KDScientific) at a flow rate of 50–100 μl min⁻¹ until all air bubbles were evacuated and the entire chip surface was wet. The nematocyst capsules were injected through the inlets of channel 1 at a flow rate of 5 μl/min and trapped in the micro-channel pockets (figure 1c). The water–oil interface was formed in the micro-channels by introducing oil through the inlets of channel 2 at a flow rate of 4 μl min⁻¹, while maintaining the water flow in channel 1. Before adding the activating solution, the flow of both water and oil was stopped. The activating solution (5 μl of 1% subtilisin; Sigma) was added through the inlet of channel 1 using a pipette. Upon activation, the capsule discharged, either back to the space of channel 1 or through the micro-channels. The dynamics of the tubule elongation was recorded using an Andor Neo sCMOS camera that was attached to a Nikon TII inverted epi-fluorescent microscope (with 10× and 20× objective lenses) at a rate of 10–200 frames per second. The length of the elongating tubule as a function of time and the rate of liquid accumulation at the tubule tip were measured using the image processing software IMAGEJ (NIH).

3. Model derivation

The proposed mechanism of the elongation process is presented here by means of a mathematical mass transport model. The model assumes that an internal pressure is responsible for the force needed to elongate the tubule and that this pressure is building up as a response to an increasing osmotic potential. Instead of limiting the osmotic potential to the nematocyst’s capsule, the model assumes that an osmotic potential is developed also along the tubule. The osmotic potential depends on the local concentration of pγGlu; as this concentration depends on the flow of the aqueous pγGlu solution through the system, we focused on formulating the water flow and pγGlu transport along the tubule. The model assumes a one-dimensional approximation and neglects molecular diffusion (the Peclet number, Pe, is approximately 1 × 10⁶ in the water–water experiments and approximately 10–150 in the water–oil experiments). As the model focuses on the tubule elongation dynamics, it does not address the initial ultra-fast stage nor the processes that take place after the tubule reaches its full length (e.g. during which liquid may exit the tubule through its openings).

The distribution of the pγGlu concentration C(x, t) along the tubule is described by the non-conservative form of the solute mass conservation equation,

\[ \frac{\partial C}{\partial t} + \frac{Q}{A} \frac{\partial C}{\partial x} + \frac{2\pi R_0 J_w}{A} C = 0, \]  

where \( Q(x, t) \) is the flow rate in the tubule, \( x \) is the axis along the tubule (figure 2), \( t \) is the time of the tubule elongation and \( A \) is the tubule cross-sectional area, assumed constant except for the change shown in figure 2b. While in figure 2a the tubule’s tail is still in the capsule and the cross-sectional area is \( A = A_1 = \pi(R_1^2 - R_2^2) \), in figure 2b the tail is already everted and is shown inside the tubule. In this case, two cross-sectional areas exist: \( A_1 \) and \( A_2 = \pi R_2^2 \) (\( R_2 \) and \( R_1 \) are the outer and inner radii, respectively). For simplicity, the water flux across the tubule wall, \( J_w \), is assumed constant along the tubule section that is immersed in water. Since no osmotic potential can develop in oil, \( J_w \) is assumed zero along the oil section. Note that at any time, \( t \), the length of the tubule from the capsule to its tail is defined as \( L_2 \) (where \( L_2 = 2L - L_{\text{end}} \)) and equation (3.1) was solved separately for \( L < L_{\text{end}}/2 \) and for \( L > L_{\text{end}}/2 \) given that \( A \) is constant for each case (\( L = L(t) \) is the instantaneous tubule length and \( L_{\text{end}} \) is its final, fully elongated, length).

**Figure 2.** A schematic of the capsule and tubule system. (a) When \( L(t) < L_{\text{end}}/2 \) and (b) when \( L(t) > L_{\text{end}}/2 \).
A solution of equation (3.1) requires an equation for the flow rate, $Q(x, t)$, and a boundary condition for $C(0, t)$. The flow rate is obtained by a solution of the mass conservation as follows:

$$\frac{\partial A}{\partial t} + \frac{\partial Q}{\partial x} - 2\pi R_0 J_0 = 0.$$  (3.2)

Given that the flow rate boundary condition at the tubule moving front is $Q(L, t) = A_1(\text{d}L/\text{d}t)$, the solution of equation (3.2) for $L(t) > L_{\text{end}}/2$ is as follows:

$$Q(x, t) = \pi(R_0^2 + R_1^2) \frac{\text{d}L}{\text{d}t} \int_x^L J_0 \text{d}x, \quad 0 < x < L_2 \quad (3.3)$$

and

$$Q(x, t) = \pi(R_0^2 - R_1^2) \frac{\text{d}L}{\text{d}t} - 2\pi R_0 \int_x^{L_2} J_0 \text{d}x, \quad x > L_2. \quad (3.4)$$

Equation (3.4) is also the solution when $L(t) < L_{\text{end}}/2$ for $0 < x < L(t)$.

To allow continuous and smooth simulations and a well-defined boundary condition at the moving tubule front, measured values of $L(t)$ were fitted to a power law,

$$L(t) = a \left( \frac{t}{L_{\text{end}}} \right)^b, \quad (3.5)$$

where $L_{\text{end}}$ is defined as the time needed for the tubule to reach a length of $L_{\text{end}} = 356–363 \mu$m for all the experiments except for the $L_{\text{end}} = 140 \mu$m experiment where the fully elongated tubule was $335 \mu$m. The curve fitting results are listed in table 1. The table shows that, except for the $L_{\text{end}} = 140 \mu$m experiment, $a$ and $b$ are almost the same in all the experiments ($a = 359.5 \pm 3 \mu$m and $b = 0.2 \pm 0.01$).

The boundary condition $C(0, t)$ is calculated by applying a mass balance inside the capsule. We assume that the capsule volume is constant and therefore the flow rate $Q_0(t) = Q(0, t)$ that exits the capsule is the same as the water flux that enters the capsule through its wall multiplied by the surface area of its envelope. By assuming perfect mixing inside the capsule, the capsule concentration $c(t)$ is described by

$$\frac{\partial (V_c c)}{\partial t} + Q_0 c = 0, \quad (3.6)$$

where $V_c$ is the capsule constant volume (assuming the capsule is a sphere) and $t$ is time. A solution of equation (3.6) results in an exponential concentration decay and was used as the boundary condition for equation (3.1),

$$C(0, t) = c(t) = c_0 \exp(-t/V_c) \int_0^t Q_0 \text{d}t. \quad (3.7)$$

Profiles of pyGlu concentration $C(x, t)$ were obtained by numerically solving equation (3.1) for each of the water–oil experiments using measured values of $L(t)$, calculation of $Q(x, t)$ by equations (3.3) and (3.4) and by applying the boundary condition obtained by equation (3.7). As will be shown, the pyGlu concentration profiles were used to calculate the forces that drive the tubule elongation in each of the experiments.

### 3.1. The numerical simulations

Equation (3.1) was solved numerically by adopting an explicit upwind scheme [18] while stepping backwards along the tubule from its moving front to the capsule. The initial concentration inside the capsule was $c_0 = 3000 \text{ mol m}^{-3}$, consisting of a $2 \text{ M}$ estimated contribution from the pyGlu and a $1 \text{ M}$ contribution from the calcium ions [19]. Note that, since equations (3.1) and (3.6) are identical when the concentration $C(x, t)$ is replaced by a non-dimensional concentration $C/C_0$, the model relative behaviour does not change when a different $C_0$ value is chosen. The capsule radius ($R_0 = 6 \mu$m) and the tubule outer radius ($R_0 = 1.15 \mu$m) were measured during the experiments but the exact inner radius of the tubule is unknown. The model results were computed by using a fixed value for $R_0 = 0.15 \mu$m and zero for $J_0$ (§4.3). The sensitivity of the model to both $R_0$ and $J_0$ was tested as reported in §4.4. Finally, the model parameters, $t_{\text{end}}$, $a$, and $b$, listed in table 1, were used in the simulations of each of the water–oil experiments.

### 4. Results

The study hypothesis states that, in addition to the wall of the capsule, the tubule wall is also an osmotic membrane, and, depending on the concentration of the aqueous pyGlu solution inside the tube, the tube has the ability to generate an osmotic potential. The following comparisons between the water–water experiments and the water–oil experiments, and the effect of the water–oil interface location, are aimed at testing the study hypothesis.

#### 4.1. Water–water experiments

To find the time needed for full tubule release, we initially tested the system in water–water conditions (figure 3). The capsule and the released tubules were surrounded by water and the length of the tubule as a function of time was measured. The results show that the tubule elongation is completed after approximately $50 \text{ ms}$, that the elongation dynamics follows a sigmoid-like behaviour, and that its maximum propagation speed (approx. $12 \text{ m s}^{-1}$) occurs at around half the total time (figure 3a). The low initial tubule elongation speed was also reported by Holstein & Tardent [11, fig. 3], which showed that, immediately after the ultrafast stage, the tube halted for about $0.15 \text{ ms}$, before moving forward again. To test the possibility that friction between the tubule and the micro-channel walls may reduce the elongation speed, we compared results that were obtained in an unconstrained water droplet with the results obtained in the microfluidic device. Figure 3e shows that both experiments generate similar results, indicating that potential friction does not play a significant role and that the

<table>
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<th>$t_{\text{end}}$ (s)</th>
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<td>361</td>
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The water–water experiments test the hypothesis that the osmotic potential along the tubule plays a crucial role in its elongation. To this end, the capsule was kept in water, whereas the tubule was released into an oil environment. While the conditions around the capsule were kept exactly the same, oil that was introduced into channel 2 eliminates the development of osmotic potential in increasing sections along the tubule. If the capsule was solely responsible for generating the osmotic potential and the tubule elongation driving force, the elongation rate in all the water–oil experiments would have been the same and equal to that of the water–water experiments. Our findings show that tubule elongation through oil is orders of magnitude slower than that through water. The elongation of the tubule in the $L_{\text{oil}} = 24\, \mu m$ experiment took 27.4 s until it was fully released (see electronic supplementary material, video, and figure 4). The video clip consists of six panels: the left panel presents one of the water–water experiments while the other five panels demonstrate the water–oil experiments of varying length, $L_{\text{oil}}$. The distance, $L_{\text{oil}}$, between the water–oil interface (marked by a yellow line in the video) and the capsule body (marked with a white dashed circle) is shown above each of the panels. The running time (s) appears in black below each of the panels and turns red when the moving front reaches its final length. Note that, while the values of $t_{\text{end}}$ listed in table 1 were defined as the time needed for the tubule to reach a fixed length, the clock in the video runs until the tubule is fully released. In addition to the elongation dynamics, the video shows that liquid bubbles are released through the far end of the tubule and along its side openings, a phenomenon that was described as a multiheded poisonous arrow [14].

The comparison between the water–water experiments (figure 3) and the water–oil experiments (figure 4) is striking. In addition to the three orders of magnitude difference in the elongation time, the results also show that the temporal elongation changes from a sigmoid-like shape (figure 3) in the water–water experiment to a power law (equation (3.5)) in the water–oil experiments (figure 4). As was demonstrated in the video clip, figure 4 shows that, as $L_{\text{oil}}$ increases, the time needed to reach a full extension decreases. Since the conditions surrounding the capsule were the same in all the experiments, this observation indicates that the tubule plays an active role in driving the release process. Viscous forces and the effect of oil viscosity alone cannot explain the results since no relative motion takes place between the tubule outer wall and the ambient oil (for more details see appendix A). At the end of the tubule elongation stage, measurements of the rate of liquid release from the tubule tip and the accumulation of the liquid bubbles provided additional evidence that osmotic potential is developing along the tubule (figure 5). If the tubule wall did not act as an osmotic membrane and no osmotic potential had been developed, then the increase rate of the bubble volume would have been constant in all the experiments. However, as shown in figure 5, the volume of the liquid bubble grows faster when $L_{\text{oil}}$ is longer (the tubule is relatively more exposed to water). Since the only difference in these experiments was the length of the tubule section that was immersed in water, these results provide another indication that the tubule wall acts as an osmotic membrane. These observations suggest a new mechanism for the tubule elongation. Upon the initiation of the tubule eversion, the high pyGlu concentration is transported from the capsule into the emerging

![Figure 3](image-url) (a) Measurements of tubule elongation as a function of time in the water–water experiments, comparing the results obtained in the microfluidic device with results obtained in an unconstrained water drop. Data are presented as the mean ± s.d., $n=5$. (b) A sequence of images taken every 5 ms showing the elongation of the tubule in one of the water–water experiments. Elongation time is shown at the bottom. Black arrows indicate the location of the tubule moving front. Injected liquid appears as a bubble near the moving front on the last image ($t = 60\, ms$), marked by an asterisk. The last image also shows that, following the release of the liquid, the tubule length is reduced.

4.2. Water–oil experiments

The water–oil experiments test the hypothesis that the osmotic potential along the tubule plays a crucial role in its elongation. To this end, the capsule was kept in water, whereas the tubule was released into an oil environment. While the conditions around the capsule were kept exactly the same, oil that was introduced into channel 2 eliminates the development of osmotic potential in increasing sections along the tubule. If the capsule was solely responsible for generating the osmotic potential and the tubule elongation driving force, the elongation rate in all the water–oil experiments would have been the same and equal to that of the water–water experiments. Our findings show that tubule elongation through oil is orders of magnitude slower than that through water. The elongation of the tubule in the $L_{\text{oil}} = 24\, \mu m$ experiment took 27.4 s until it was fully released (see electronic supplementary material, video, and figure 4). The video clip consists of six panels: the left panel presents one of the water–water experiments while the other five panels demonstrate the water–oil experiments of varying length, $L_{\text{oil}}$. The distance, $L_{\text{oil}}$, between the water–oil interface (marked by a yellow line in the video) and the capsule body (marked with a white dashed circle) is shown above each of the panels. The running time (s) appears in black below each of the panels and turns red when the moving front reaches its final length. Note that, while the values of $t_{\text{end}}$ listed in table 1 were defined as the time needed for the tubule to reach a fixed length, the clock in the video runs until the tubule is fully released. In addition to the elongation dynamics, the video shows that liquid bubbles are released through the far end of the tubule and along its side openings, a phenomenon that was described as a multiheded poisonous arrow [14].

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Figure 5. The time evolution of the liquid volume, injected from the tubule far end in the water-oil experiments. The measured time starts after the tubule elongation is completed.

tubule. Over time, the concentration of pGlu in the capsule decreases as the length of the tubule increases, diminishing the pGlu concentration at the entrance to the tubule. This mass transfer process results in a non-uniform concentration distribution along the tubule, maintaining its highest concentration at the moving front with a decreasing concentration profile towards the capsule.

4.3. The mathematical model

The model computes the processes that cannot be measured inside the nematocyst. These include the longitudinal and temporal variations in flow rate and concentration inside the elongating tubule, the distribution of internal pressure and the resulting driving force. Using the measured length and internal geometry of the tubule, the model computes the flow rate that exits the capsule and enters the tubule, \( Q(t) \). Assuming fully mixed conditions inside the capsule, the solution of equation (3.6) results in an exponential decay of the capsule pGlu concentration (equation (3.7)) that is required as a boundary condition for the mass conservation equation, equation (3.1). Equation (3.7) starts with the initial concentration, \( C_0 \), and decreases at a rate that depends on the flow rate through the capsule wall, \( Q(t) \). The flow rate along the tubule, \( Q(x, t) \), is calculated using equations (3.3) and (3.4). The time-dependent concentrations at the water-oil interface, \( C(L_{oil}, t) \), are obtained by numerically solving equation (3.1). The force that drives the tubule elongation was calculated by identifying the relevant pGlu concentration. When the moving front of the tubule is in water, the driving concentration \( C_{drive} \) is at the moving tubule front such that \( C_{drive} = C(L, t) \). Once the front crosses the water-oil interface \( x = L_{oil} \) the driving concentration is calculated at the interface, \( C_{drive} = C(L_{oil}, t) \), assuming that the maximal osmotic pressure exists along the entire length of the tubule that is immersed within the oil phase.

The flow rate of \( L_{oil} = 65 \mu m \), calculated by equations (3.3) and (3.4), at five different times \( t_i \) is presented in figure 6. It shows that the flow rate is decreasing with time and is uniform along the tubule except for a step decrease that occurs due to the sudden change in the cross-sectional area at the trailing end of the tubule. This sudden change is missing in the \( t_1 / t_{end} = 0.025 \) case as the tubule end is still inside the capsule. Starting with \( t_2 / t_{end} = 0.05 \), all the cases display the sudden change as the trailing end is inside the tubule. Figure 6 also shows that the location of the water-oil interface does not affect the flow rate since \( f_{c0} \) was assumed to be zero in these simulations.

As opposed to the longitudinal uniformity in flow rate, figure 7a shows that the pGlu concentration is increasing along the tubule, reaching a maximum at its moving front. The reason for this is the exponential concentration decrease at \( x = 0 \) (see the left end of the concentration profiles) and the advection caused by \( Q(x, t) \). At \( t = 0 \), the pGlu concentration in the capsule is the highest \( (c_0) \). As time evolves, the concentration of pGlu in the capsule, \( c(t) \), is decreasing and lower values enter the tubule while pushing the pGlu solution forward. From the concentration profiles that are shown in figure 7a, we have a special interest in the temporal behaviour of the concentration at the water-oil interface, \( C(L_{oil}, t) \). \( L_{oil} \) is the last location where osmotic potential can develop and where the tubule elongation driving force is determined. An example of the concentration decrease at \( x = L_{oil} \) is shown in the inset. The temporal change of this concentration is similar to the temporal change of driving forces shown in figure 7b.

The force that drives the tubule elongation is a product of the concentration-dependent pressure \( P_{drive} \) and the annular cross-sectional area at the moving front, \( A_t \),

\[
F = P_{drive} A_t. \tag{4.1}
\]

The driving pressure \( P_{drive} \) is estimated by a formulation commonly used when modelling the flow of a permeate in osmotic membrane systems [20],

\[
J_w = \alpha (\Delta \pi - \Delta P), \tag{4.2}
\]

where \( \alpha \) is a water permeability membrane coefficient, \( \Delta P \) is the difference in internal pressure \( (\Delta P = P_i - P_o) \) and \( \Delta \pi \) is the osmotic potential across the tubule wall \( (\Delta \pi = \pi_i - \pi_o) \), where the subscripts \( i \) and \( o \) are inner and ambient, respectively. Note that \( J_w \) is positive against the radial direction,
i.e. positive from outside in. When $\Delta P = \Delta \pi$, no water crosses the wall ($J_w = 0$) and the internal pressure increases to its highest potential value. For a given $J_{\text{in}}/\alpha$, the pressure $P_i$ can be calculated by a combination of equation (4.2) and the Morse equation,

$$\pi(x, t) = iRTC(x, t),$$

which is valid for dilute solutions. $T$ is temperature (taken here as 293 K), $R$ is the gas constant and $i$ is the van’t Hoff factor, taken as unity. Using equations (4.1)–(4.3) and setting $P_a$ and $\pi_a$ to zero, the tubule elongation force is

$$F = \left(\frac{RTC_{\text{drive}} - \frac{J_w}{\alpha}}{\alpha}\right)A_1,$$

where $C_{\text{drive}}$ depends on the experimental conditions (e.g. the location of $L_{\text{end}}$). Figure 7 shows that the location of the oil interface determines the pyGlu concentration that drives the tubule. For longer $L_{\text{end}}$ lengths, the greater the driving force and the eversion speed are. When no oil interface exists, the driving force depends on the concentration at the far end of the tubule. Assuming no diffusion and no dilution with water ($J_w = 0$), the concentration at the moving front (figure 7a) and the driving force in the water–water case is constant.

Note that the inner folded tubule section moves at twice the speed of the tubule front and, as a result, these forces are double what would have been needed if the tubule had not been everted inside out. This is analogous to pulley lift systems that apply only half the object weight, compensated by the double distance of the system chain. In order to generate such large forces, a high concentration and large osmotic potential must be developed at the tubule front.

4.4. Sensitivity analysis

Except for the inner tube diameter ($R_i$) and the water flux across the tubule wall ($J_{\text{in}}$) all the other model parameters were either measured or reported in the literature (e.g. [21]). The model results shown so far (figures 6 and 7) assumed a radius ratio $R_i/R_0 = 0.13$ and $J_{\text{in}} = 0$. In the following, we test the sensitivity of the model to a range of $R_i$ and $J_{\text{in}}$ values.

The influence of $J_{\text{in}}$ on the flow rate and the distribution of pyGlu for the $L_{\text{end}} = 65 \mu$m experiment are shown in figure 8. These results were obtained for a radius ratio of 0.13 and are shown for $t/t_{\text{end}} = 0.99$, towards the end of the elongation process. Since $J_{\text{in}}$ was assumed constant along the tubule, the flow rate varies linearly with $x$ and is constant when the osmotic potential and $J_{\text{in}}$ are zero in the oil. It was
driving force. This concentration profile depends on \( J \), the moving front, is important since it defines the elongation of the tubule at two times, \( t = t_a \) and \( t = t_b \). This implies that the ambient regions that affect the capsule, a result that the model did not address. Figure 9 shows that high \( R/R_o \) ratios result in higher concentrations at both the capsule exit and along the tubule. The concentration jump at \( x = L_2 \) due to the change in flow rate. Tardent [4, fig. 2f] suggests that the radius ratio is smaller than 0.4. The sensitivity analysis presented in figure 9b indicates that the concentration profile is not very sensitive and that the concentration jump is negligible when the radius ratio is within this range.

found that, for these conditions, a water flux \( f_w \) greater than 77 nm s\(^{-1}\) generates a negative flow, namely from the tubule to the capsule. We chose to limit the analysis to positive flow rates; however, we present in figure 8a the flow rate for \( f_w = 80 \) nm s\(^{-1}\) where it is positive everywhere except for a small section near the capsule (note that a negative flow will generate an increasing (or constant) \( J \) concentration inside the capsule, \( C(t) \), and hence the concentration along the tubule, \( C(x,t) \)). Figure 9b shows that high \( R/R_o \) ratios result in higher concentrations at both the capsule exit and along the tubule. The concentration jump at \( x = L_2 \) is due to the change in flow rate. Tardent [4, fig. 2f] suggests that the radius ratio is smaller than 0.4. The sensitivity analysis presented in figure 9b indicates that the concentration profile is not very sensitive and that the concentration jump is negligible when the radius ratio is within this range.

5. Summary

Our new mechanistic explanation suggests that the elongation driving force is equal to the product of the concentration-dependent pressure and the annular cross-sectional area at the tubule moving front. Once it crosses the water–oil interface, it loses its ability to pull the tubule since no osmotic potential can be developed in oil. Therefore, the location of the interface determines the \( J \) concentration inside the capsule, \( (t) \), and hence the concentration along the tubule, \( C(x,t) \). Figure 9b shows that high \( R/R_o \) ratios result in higher concentrations at both the capsule exit and along the tubule. The concentration jump at \( x = L_2 \) is due to the change in flow rate. Tardent [4, fig. 2f] suggests that the radius ratio is smaller than 0.4. The sensitivity analysis presented in figure 9b indicates that the concentration profile is not very sensitive and that the concentration jump is negligible when the radius ratio is within this range.

Figure 9. The effect of the radius ratio \( R/R_o \) on (a) the flow rate and (b) the \( p \) concentration for the \( L_{\text{end}} = 65 \) \( \mu \)m experiment. The vertical dashed line marks the water–oil interface.

Figure 10. A schematic of the inside-out eversion: (a) and (b) represent the tubule at two times, \( t_a \) and \( t_b \), where the red line marks the tubule elongated length at \( t = t_a \).
such as protection against jellyfish stinging. These new findings facilitate our understanding of potential prey defense strategies (such as the release of mucus or high osmotic solutions), but may also facilitate the development of osmosis-based methods for nanotube production and drug delivery [22–24].

Competing interests. We declare we have no competing interests.

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Appendix A. The role of oil viscosity

In this appendix, we investigate the potential role of the oil viscosity. As will be shown, it cannot explain the slowing down observed in the water–oil experiments when compared with the water-only experiments. The main mechanism through which viscosity could impose a resisting force is a shear stress that hypothetically develops along the tubule external walls. Since the tubule is released by an inside-out eversion, the tubule wall of the already unfolded part does not move with respect to the ambient fluid (assuming zero motion of the nematocyst as a whole). Figure 10 illustrates the inside-out eversion and shows how the tubule lays its outer wall in the ambient fluid. As an analogy this is similar to the action of a vehicle with caterpillar treads when it moves forward and lays its tracks on the ground; however, as opposed to the vehicle with caterpillar treads that uses friction with the ground to move forward, the elongation driving force in the nematocyst is internal. As a result, no shear stress is generated and viscosity has no role to play. The only location where viscosity might have an influence is at the moving tubule tip. Although the rolling out of the tip might generate a small vortex ring, we chose, for simplicity, to approximate the influence of viscosity at the tubule tip by using Stokes’ law, $F_{\text{visc}} = 6 \pi \mu R_{t} (dL/dt)$, $Re \ll 1$. Using table 1, we estimate the viscous force that resists the tubule tip as $F_{\text{visc}} \approx 8.2 \times 10^{-8} - 1.7 \times 10^{-5} \mu N$ when the viscosity is that of water ($\mu = 0.001 \text{ kg m}^{-1} \text{s}^{-1}$). The estimated $F_{\text{visc}}$ is orders of magnitude smaller than the force shown in figure 7b. Since the dynamic viscosity ($\mu$) of the oil (light mineral oil; Sigma-Aldrich-330779) was only approximately 13 times higher than that of water, $F_{\text{visc}}$ cannot explain the orders of magnitude reduction in elongation speed.

Finally, in order to demonstrate the negligible role of viscosity, we tested the tubule elongation rate while using a low-viscosity oil (Fluorinert FC-40; Sigma-Aldrich; $\nu = 2.2 \text{ cSt}$, $\mu = 3.34 \text{ cP}$). Since the experiment involved a new batch of nematocysts, we tested again the elongation rate with the light mineral oil ($\nu = 15.6 \text{ cSt}$, $\mu = 13 \text{ cP}$).

Table 2 shows that the time needed to complete the elongation ($t_{\text{end}}$) is approximately the same regardless of the viscosity of the oil. Regardless of the type of the ambient oil, the values of $t_{\text{end}}$ in table 2 (4.5–5.5 s) are bounded between the $t_{\text{end}}$ in the $L_{\text{oil}} = 70 \mu m$ experiment (9.3 s) and the $t_{\text{end}}$ in the $L_{\text{oil}} = 85 \mu m$ experiment (3.2 s) as reported in table 1. We, therefore, conclude that the ambient fluid viscosity cannot explain the large reduction in the tubule elongation rate that we found in this study.

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